Match 3 Round 1

Arithmetic: Bases and Scientific Notation

- 1.) _____
- 2.)
- 3.)

<u>Please Note</u> The symbol 12_B represents a 2-digit number in base B.

1.) Express $\frac{\left(12\cdot10^{18}\right)\left(20\cdot10^{9}\right)\left(15\cdot10^{11}\right)}{\left(24\cdot10^{25}\right)}$ in scientific notation.

2.) Simplify $(30\cdot10^6)(20\cdot10^{14})(30\cdot10^{-21})$ and express your answer as a base 5 numeral.

3.) Calculate $1248_{16} + 421_8$. Express your answer as a base 4 numeral.

2011-2012

FAIRFIELD COUNTY MATH LEAGUE (FCML) 29192000

Name	TANK MOUTH
Match 3 Round 2	
Algebra I: Word Problems	1.)
	2.)
	2 \
•	3.)

1.) Mixture A contains 100% juice. Mixture B contains 80% juice and 20% water. If there are 100 L of each mixture available, how many liters of a mixture containing 98% juice and 2% water is it possible to make?

2.) Adding their scores, Ellen and Kelly scored a total of 114 points on the first assignment. Ellen scored 13 more points on her second assignment than on her first assignment. Kelly scored 11 fewer points on her second assignment than on her first assignment. If Kelly scored four more points on her two assignments than Ellen scored on her two assignments, then find how many points Kelly scored on her first assignment.

3.) Working together, Al and Bob can complete a job in 2 days. It takes Bob and Charlie three days working together to complete the same job. Working together, it takes Al and Charlie 4 days to complete the same job. How many days will it take to complete the same job if Al, Bob, and Charlie all work together?

Match 3 Round 3 Geometry: Polygons	1.)	
	2.)	
	3.)	
1.) List all possible values for than three times its exterior a	or n such that a regular n -gon has interior angles that are leangles.	ess
2) A regular polygon with 1	4 diagonals shares a side with a regular polygon with 9 si	dos
	h of 7, then what is the perimeter of the polygon which is	
H has six sides. The ratio of ratio of the perimeter of H to	sides, regular polygon S has four sides, and regular polyg the apothem of T to the apothem of H is the same as the othe perimeter of S . If the area of T is the same as the apothem of H to the apothem of S .	

Match 3 Round 4

Algebra II: Functions and Inverses

1 \		
1.)		
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2.)

3.)

1.) The function g has the property that g(x) = 1 + g(x - 1) for all real x, and g(0) = 1. The function f is defined by f(x) = x + g(x). Evaluate f(10).

2.) Let $f(x) = x^2 - 4$, g(x) = x + 3, and $h(x) = \frac{f(g(x))}{g(f(x))}$ for all x > 1. Simplify h(x).

3.) If the function f is defined by $f(x) = \frac{1}{\sqrt{4-x^2}}$, then what is the domain of the function $f \circ f$?

[Explanation of notation: For any function f, the function $f \circ f$ is defined by $f \circ f(x) = f(f(x))$, for all values of x for which f(f(x)) is real.]

Match 3 Round 5

Advanced Topics: Exponent and Log

Expressions and Equations

1.)

2.)

3.)

1.) Evaluate $\frac{\log 8}{\log(\frac{1}{4})}$.

2.) Solve for *x*: $1 + \log_3 x = \log_x 9$

3.) Given that $2^{5x+2y} = 2^{3x} + 2^{3x+3}$ and $3^{-3x} = 3^{3y} - 3^{-3x-2}$, evaluate $(12)^{3x+3y}$

Match 3 Round 6

Discrete Math: Matrices

2.)

3.)

1.) If
$$\begin{bmatrix} 10x & 1 \\ -4 & 4z \end{bmatrix}$$
 $\cdot \begin{bmatrix} 6 & -3 \\ 30y & 5 \end{bmatrix} = \begin{bmatrix} 0 & -9 \\ \frac{-36}{5} & 9 \end{bmatrix}$, then find $x + y + z$.

2.) Find the determinant of
$$\begin{bmatrix} 187 & 189 \\ 191 & 193 \end{bmatrix}$$
.

3.) If
$$A = \begin{bmatrix} -4 & 4 \\ 1 & -2 \end{bmatrix}$$
 and $A \cdot X \cdot A = \begin{bmatrix} 2 & 0 \\ 1 & 1 \end{bmatrix}$, then find X .

Match 3 Team Round

- 1.) Compute $FCML_{30} + MATH_{30}$. Write your answer in base 30.
- 2.) Six grams of the color Aqua is made from mixing 5 grams of blue with 1 gram of green. Three grams of the color Sea Gold is made from mixing 2 grams of blue with 1 gram of green. Five grams of the color Turquoise is made from mixing 4 grams of blue with 1 gram of green. Dave had just enough materials to make 40 grams of Aqua and 15 grams of Sea Gold. How many grams of Turquoise could he have made, discarding any leftover materials?
- 3.) There are two regular n-gons such that the interior angle of the regular n-gon is $(10n)^{\circ}$ more than its exterior angle. Find the positive difference between the number of diagonals in the two n-gons.
- 4.) If f(x+10) = 2x+6, then find all values of x such that $f(x) = f^{-1}(x)$.
- 5.) If $a = \log_5 4$ and $b = \log_8 27$, then evaluate $\left(5^a 2^b\right)^2$.

6.) If
$$M = \begin{bmatrix} a & 0 & b \\ b & -b & a \\ 0 & b & b \end{bmatrix}$$
 and $N = \frac{1}{5} \cdot \begin{bmatrix} c & -b & -b \\ b & -a & c \\ -b & a & a \end{bmatrix}$ are inverses, and $P = \begin{bmatrix} a & 0 \\ b & b \end{bmatrix}$ and

 $Q = \frac{1}{2} \cdot \begin{bmatrix} b & 0 \\ -b & a \end{bmatrix}$, then find all possible ordered triplets (a,b,c). (P and Q are inverses)